Title: Electrolytic Fluid Speciation by Gibbs Energy Minimization and Implications for Subduction Zone Mass Transfer

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Abstract: The number of solute species required to describe the thermodynamic behavior of electrolytic fluids is a hindrance to the incorporation of aqueous geochemistry in petrological Gibbs energy minimization procedures. An algorithm is developed to overcome this problem. Beginning from the solute-free limit, chemical potentials and phase stability are determined by minimization, the solute speciation and bulk fluid properties consistent with these chemical potentials are then computed and the procedure repeated until the chemical potentials converge. Application of the algorithm to a model for metamorphism of subduction sediment shows that accounting for solute chemistry does not change the conclusion based on molecular fluid models that a pervasive water flux from the subjacent mantle is required to explain island-arc CO_2 emissions by fluid-mediated slab decarbonation. This putative flux would deplete the sediment in potassium, rendering the slab refractory to melting and limiting its capacity to transport water to greater depth.

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Dear EPSL:

Herewith please find a manuscript on a method for incorporating electrolytic fluid speciation in Gibbs energy minimization calculations and its application to subduction zone mass transfer that I submit for your consideration as a publication in EPSL.

It is difficult to place this work fairly in scientific context because existing Gibbs energy minimization codes (e.g., Harvie et al. 1987; Karpov et al., 2001) already have the capability to treat electrolytic fluids robustly. The limitations of the existing codes are practical rather than algorithmic. In contrast, the algorithm developed and implemented in this paper is imperfect, but it makes practical a broad spectrum of geochemical problems that are not currently tractable. Rather than bore the reader with lists of technicalities about what program X can do, but program Y cannot do, I have demonstrated the capabilities of the method through an application to subduction zone mass transfer.

The thermodynamic data necessary for the application to subduction zones is highly uncertain, but I believe the results have scientific value. Specifically, these results suggest that: 1) solute chemistry increases carbon solubility in subduction zone fluids by roughly a factor of two; 2) fluid-mediated decarbonation of subducted oceanic crust requires water infiltration from an external source; 3) that such an infiltration event would have profound geochemical consequences, notably K depletion; and 4) that subducted sulfides become soluble by the reduction of carbonate to produce diamond.

Sincerely,

James A. D. Connolly

Highlights:

- Electrolytic fluid speciation is implemented in a Gibbs energy minimization code.

- Dissolution increases C-solubility two-fold compared to molecular fluid models.

- Infiltration-driven decarbonation desiccates the crust by K-depletion.

- Sulfides become soluble by the reduction of carbonate to diamond at ~6 GPa.

1   # Electrolytic Fluid Speciation by Gibbs Energy Minimization and

2   # Implications for Subduction Zone Mass Transfer

3

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9   ## Abstract

10   The number of solute species required to describe the thermodynamic behavior of electrolytic

11   fluids is a hindrance to the incorporation of aqueous geochemistry in petrological Gibbs energy

12   minimization procedures. An algorithm is developed to overcome this problem. Beginning from

13   the solute-free limit, chemical potentials and phase stability are determined by minimization, the

14   solute speciation and bulk fluid properties consistent with these chemical potentials are then

15   computed and the procedure repeated until the chemical potentials converge. Application of the

16   algorithm to a model for metamorphism of subduction sediment shows that accounting for solute

17   chemistry does not change the conclusion based on molecular fluid models that a pervasive

18   water flux from the subjacent mantle is required to explain island-arc CO_2 emissions by fluid-

19   mediated slab decarbonation. This putative flux would deplete the sediment in potassium,

20   rendering the slab refractory to melting and limiting its capacity to transport water to greater

21   depth.

22

25

1. Introduction

Gibbs energy minimization is applied to a broad spectrum of geochemical and petrological problems (Leal et al., 2017). In geochemistry the focus of these applications is usually modelling reactive transport (Wolery, 1992; Bethke, 1996), whereas in petrology the focus is predicting phase stability (DeCapitani and Brown, 1987; Connolly, 2009). This disparity has led to a situation in which geochemical codes account for complex fluid chemistry, but often seek only a local equilibrium solution, whereas petrologic codes seek a costly global solution that limits their ability to treat the complex fluid chemistry. As a means of bridging this gap Galvez et al. (2015; Galvez et al., 2016) use phase equilibria computed by Gibbs energy minimization assuming a solute-free fluid to back-calculate solute chemistry. This method accurately estimates solute chemistry provided the solute mass is small compared to the total mass of the system, but is not well suited for reactive transport problems because the phase proportions and bulk fluid chemistry are not rigorously determined. The present work improves on this method by incorporating back-calculated fluid chemistry in an iterative Gibbs energy minimization procedure referred to here as lagged speciation.

The utility of the lagged speciation algorithm is demonstrated by a model for devolatilization of subduction zone sediments. This problem has been made tractable by the Deep Earth Water (DEW) model for electrolytic fluids (Sverjensky et al., 2014), which extends the Helgeson-Kirkham-Flowers (HKF) formulation (Shock and Helgeson, 1988) for aqueous species to high pressure conditions. Although a number of studies have considered the implications of the DEW model for fluid-dominated subduction zone chemistry (Facq et al., 2014; Sverjensky and Huang, 2015; Tumiati et al., 2017), the present focus is the rock-dominated limit appropriate in systems where the fluid is generated by devolatilization. This limit was investigated by Galvez et al. (2015) using a variant of the DEW model. The distinction between the DEW model and the

51   Galvez et al. (2015) variant, is that in the DEW model the solvent is H_2O and molecular volatiles

52   are treated as solute species, whereas in Galvez et al. (2015) the solvent is a mixture of

53   molecular volatiles. Both approaches are compared.

54

55   Subduction zone devolatilization is topical because of its potential role in various global element

56   cycles. The observation, based on simple sub-solidus phase equilibrium models (Kerrick and

57   Connolly, 2001ab) that carbonates persist within subducted slabs beyond sub-arc depth has

58   motivated alternative hypotheses to explain extensive slab decarbonation and/or island-arc

59   emissions. These hypotheses include: infiltration-driven decarbonation (Connolly 2005; Gorman

60   et al., 2006); carbon transfer by entrainment or diapirism (Dasgupta et al., 2004; Behn et al.,

61   2011); slab-melting (Poli, 2015; Skora et al., 2015); or near-surface provenance volcanic CO_2

62   (Mason et al., 2017). With the exception of the latter, all of these mechanisms are viable but

63   unsatisfying in that they require a coincidence of processes or extreme temperatures. Evidence

64   of subsolidus carbonate dissolution (Frezzotti et al., 2011; Ague and Nicolescu, 2014) has

65   prompted the suggestion that, by neglecting the solubility of non-volatile elements, early models

66   underestimated the efficacy of simple decarbonation processes. Previous work (Kelemen and

67   Manning 2015; Galvez et al., 2015) suggests that at typical subduction zone conditions

68   dissolution causes a two-fold increase in the carbon content of subduction zone fluids, but does

69   not address fluid production. The models here extend that work by tracking fluid evolution from

70   the surface to beyond sub-arc depths.

71

72   This paper begins with a generalization of the back-calculation method (Galvez et al., 2015).

73   The lagged speciation algorithm by which back-calculated results may be integrated into a

74   Gibbs energy minimization procedure is then outlined and the limitations of the algorithm are

75   explained. The final major section uses the subduction zone model to illustrate some

76   technicalities of the method and to explore the consequences of solute chemistry on closed,

77   open, and infiltration-driven devolatilization scenarios.

2. Back-Calculated Speciation

79   Back-calculated speciation designates the calculation of the solute speciation of an electrolytic

80   fluid under the assumptions of charge balance, equilibrium, known solvent composition, and

81   specified chemical potentials. The partial molar Gibbs energy of any species can be expressed

82   as

83    $$g^i = -n^i_{e-}\mu_{e-} + \sum_{j=1}^{c} n^i_j \mu_j \qquad\qquad 1$$

84   where c is the number of components, μ_i and μ_{e-} are, respectively, the chemical potential of

85   component j and the electron, and for species i: n^i_j is the molar amount of component j and $-n^i_{e-}$

86   is the molar charge, abbreviated hereafter q^i. Equation 1 can be rearranged to express μ_{e-} in

87   terms of the chemical potentials and the properties of charged species i

88    $$\mu_{e-} = \frac{1}{q^i}\left(g^i - \sum_{j=1}^{c} n^i_j \mu_j \right). \qquad\qquad 2$$

89   Because μ_{e-} is the same for all species at equilibrium, equating the right-hand-side of Equation 2

90   for two distinct charged species yields a relation between the partial molar Gibbs energy of any

91   arbitrarily chosen charged species and the partial molar Gibbs energy of a charged reference

92   species k

93    $$g^i = \frac{q^k}{q^i}\left(g^k + \sum_{j=1}^{c} \mu_j \Delta n^i_j \right) \qquad\qquad 3$$

94   where $\Delta n^i_j = n^k_j - n^i_j$. In terms of a solute reference state activity model, the partial molar Gibbs

95   energies in Equation 3 are

96    $$g^i = g^{*,i} + RT \ln\left(m^i \gamma^i \right) \qquad\qquad 4$$

97   where $g^{*,i}$ is the solute reference state molar Gibbs energy; m^i is the molal concentration, γ^i is

98   the activity coefficient, T is temperature, and R is the universal gas constant. Substituting

99   Equation 4 into Equation 3 and rearranging the result

100   $$m^i = \frac{c^i}{\gamma^i}\left(m^k\gamma^k\right)^{q^k/q^i}$$ 5

101   where

102   $$c^i = \exp\left(\frac{q^k}{q^i}\left[g^{*,k} + \sum_{j=1}^{c}\mu_j\Delta n^i_j\right] - g^{*,i}\Big/ RT\right).$$

103   Substituting Equation 5 into the charge balance constraint for a fluid with s charged solute

104   species

105   $$\sum_{i=1}^{s} q^i m^i = 0$$ 6

106   yields

107   $$\sum_{i=1}^{s}\frac{q^i c^i}{\gamma^i}\left(m^k\gamma^k\right)^{q^k/q^i} = 0,$$ 7

108   which can be solved in the ideal limit ($\gamma^i \to 1$) for m^k if the composition of the solvent, which

109   influences $g^{*,i}$, is known. The concentrations of the remaining charged species are then

110   obtained from Equation 5 and those of neutral species from Equation 4. In the non-ideal case,

111   additional assumptions are necessary to compute the activity coefficients. Regardless of those

112   details, the flaw in this method is that if the solvent composition is consistent with the specified

113   chemical potentials, as is the case when the chemical potentials and solvent composition are

114   obtained by Gibbs energy minimization, then finite solute concentrations violate this

115   consistency. This flaw has the consequence that, except in the limit of infinite dilution ($m^i \to 0$),

116   there is no bulk fluid composition that simultaneously satisfies Equation 7 and the constraint on

117   the chemical potentials of the system.

3. The Lagged Speciation Algorithm

119   The limitation of simple back-calculated speciation is the absence of a relation between the

120   calculated solute chemistry and the bulk chemistry of the fluid, which precludes evaluation of

121   mass balance constraints. To circumvent this limitation, the present work exploits the iterative

122   aspect of Gibbs energy minimization by successive linear programming (Connolly 2009). The

123   essential feature of successive linear programming is that an initial result in which the

124   compositions of the phases are discretized at some specified resolution is iteratively refined until

125   a desired target resolution has been achieved. The innovation here is to use a minor

126   modification of the back-calculated speciation algorithm to estimate the Gibbs energy and

127   composition of the stable fluid(s). In the initial optimization, the fluid may contain multiple solvent

128   species (e.g., H_2O, CO_2, CH_4, H_2S), but is solute-free. Given the solute-free solvent

129   composition(s) and chemical potentials obtained in this optimization, the reference state solute

130   partial molar Gibbs energies are computed, Equation 7 is solved for the concentration of the

131   reference ion, and Equations 4 and 5 are solved for the concentrations of the remaining solute

132   species. The solvent mole fractions are then recomputed as

133    $$y^i_{h+1} = \frac{m^i_h}{m_{total}} \quad i = s+1,\ldots,r \qquad\qquad 8$$

134   with

135    $$m_{total} = \sum_{i=1}^{s} m^i_h + \sum_{i=s+1}^{r} y^i_h \;. \qquad\qquad 9$$

136   where r is the number of solvent species, h indexes the iteration level. The Gibbs energy and

137   bulk composition for the fluid used in the succeeding iteration are

138    $$g_{h+1} = \sum_{i=1}^{s}\left(m^i_h\left[g^{*,i} + RT\ln\left(m^i_h\gamma^i_h\right)\right]\right) + \sum_{i=s+1}^{r}\left(m^i_h\left[g^{0,i} + RT\ln\left(y^i_{h+1}\gamma^i_{0,h}\right)\right]\right) \qquad\qquad 10$$

139    $$n_{j,h+1} = \sum_{i=1}^{s} m^i_h n^i_j + \sum_{i=s+1}^{r} m^i_{h+1} n^i_j \quad j = 1,\ldots,c\,. \qquad\qquad 11$$

140 where $\gamma_{0,h}^i$ is the activity coefficient of solvent species *i* in the solute-free solvent. Equation 10

141 ignores the dependence of the solvent species activity coefficients on solute concentration and

142 is therefore thermodynamically consistent only in the ideal limit (e.g., Wolery 1990). Although it

143 is not algorithmically required, the inconsistent form is maintained because electrolytic fluid

144 species activity models are currently poorly constrained. In contrast, molecular fluid equations of

145 state are capable of predicting species activities in the solute-free solvent with good accuracy

146 (Prausnitz, 1969). Excepting this inconsistency, and in contrast to simple back-calculation,

147 iterative application of Equation 10 reaches a thermodynamically consistent solution provided

148 the lagged chemical potentials, used to compute the solute molalities m_h^i by back-calculation,

149 converge.

3.1 Algorithmic Limitations

151 Because the lagged speciation algorithm predicts fluid composition from a back-calculated

152 result convergence to a stable solution is not guaranteed. The condition for algorithmic failure is

153 that no combination of phases involving the solute-bearing fluid simultaneously satisfy mass

154 balance and minimize the Gibbs energy of the system. This condition may be manifest in two

155 distinct ways which are outlined in detail below because the ability to recognize failure is

156 essential for the practical implementation of an imperfect algorithm.

157

158 The more easily understood manifestation of algorithmic failure is illustrated schematically for

159 the H_2O-SiO_2 system at conditions where, depending on bulk composition, the stable phase

160 assemblages are quartz (q) + fluid (F) or fluid (Fig 1). For any general composition, the initial,

161 solute-free, optimization identifies q + pure-water (H_2O) as the stable phase assemblage.

162 Simple back-calculation from this result corresponds to a Gibbs-energy composition coordinate

163 (blue, Fig 1a) on the line connecting the coordinates of quartz and pure-water, whereas the

164 coordinate computed by lagged speciation (Eqs 8 and 9) must lie below this line, at least in the

165   ideal limit. If the bulk composition of the system is more silica-rich than the fluid the iteration

166   proceeds stably because the assemblage q + F provides a physically meaningful basis for

167   estimating the chemical potentials of the system. However, if the bulk composition lies on the

168   water-rich side of the fluid composition, the successive optimization will identify F + H_2O as the

169   stable phase assemblage. This assemblage does not correspond to a real phase assemblage

170   and therefore provides no basis for refining the chemical potentials of the system in the

171   subsequent iteration. A more insidious problem is that the chemical potential of H_2O for this

172   pseudo-phase assemblage must be equal to the partial molar Gibbs energy of pure water. Thus,

173   the fluid speciation obtained by back-calculation recovers the simple back-calculated result and

174   subsequent iterations will oscillate between these solutions. The condition for algorithmic

175   stability deduced from this behavior is that if an element is represented in the fluid only by solute

176   species, then this element must be present in at least one stable phase other than the fluid. For

177   example, if K dissolves in the fluid only as a solute species, the lagged speciation algorithm will

178   fail when K is dissolved entirely in the fluid.

179

180   In systems with more than one solute-component algorithmic failure can be manifest in an

181   additional way that is illustrated schematically for the H_2O-$CaSiO_3$-SiO_2 system at a condition at

182   such that wollastonite (wo) + quartz stably coexist (Fig 2a). Assuming Ca and Si can be present

183   in the fluid only as solute species, then, for any general composition, the initial optimization will

184   identify wollastonite + quartz + H_2O as the stable phase field. Lagged speciation then identifies

185   the composition of the fluid that coexists with wollastonite + quartz (F in Fig 2b), and in the next

186   iteration there, from the algorithmic perspective, three prospective phase fields: wo + q + F; wo

187   + H_2O + F; and q + H_2O + F. The latter two fields do not correspond to real phase assemblages

188   and provide no basis for refining the chemical potentials of the system. Thus, the iteration

189   scheme becomes unstable if the systems composition lies within these fields.

190

191   Both of the preceding examples illustrate the rock-dominated limit of Galvez et al. (2015).

192   Formally, in simple back-calculation the only robust formulation of this limit is that solute

193   concentrations are negligible. As such the limit is unduly restrictive and has little practical utility

194   other than to indicate that back-calculation is likely to be accurate if the fluid mass is small. The

195   utility of incorporating back-calculated speciation in a Gibbs energy minimization procedure, is

196   that the minimization procedure automatically evaluates mass balance constraints and thereby

197   quantitatively determines the rock-dominated limit. Within this limit, the lagged-speciation

198   algorithm is unconditionally stable.

4. Devolatilization of Subduction Zone Sediment

200   To provide a minimal, but representative, model for subduction zone devolatilization the

201   geotherm (Fig 3) adopted here represents subduction of a young (40 Ma) slab at a rate of 10

202   cm/y and a kinematically prescribed dip of 45° (Rupke et al., 2004). The age and rate differ

203   slightly from the global mean (~55 Ma and ~6 cm/y) and the dip is roughly the median of

204   observed slab dips (Stern, 2002). Sediment lithologies are heterogeneous, rather than consider

205   this compositional spectrum, the global average marine sediment (GLOSS, Plank and

206   Langmuir, 1998) composition is adopted as being representative (Table 1). Previous phase

207   equilibrium modeling (Kerrick and Connolly, 2001a) indicates that the high water content of the

208   GLOSS composition favors decarbonation at low temperature compared to water-poor

209   carbonate sediments and as such provides a best case scenario for sub-arc decarbonation.

210   Because the GLOSS average does not quantify the redox state of iron or carbon, the initial bulk

211   oxygen content is computed under the assumption that all iron is ferrous and all carbon is

212   present as carbonate, a configuration identified here as the neutral bulk redox state. In the

213   resulting models, the stability of ferric iron in low-temperature minerals has the consequence

214   that a small amount of carbonate is reduced to form graphite at surface conditions and graphite

215   or diamond persists, except in the infiltration model, as a stable phase at all conditions.

216   Preliminary calculations demonstrated that an implausible initial ferric/ferrous ratio of ~2.5 would

217   be necessary to completely suppress the stability of reduced carbon during devolatilization. At

218   the opposite extreme, essentially all the initial carbon must be reduced to destabilize carbonate.

219   This extreme leads to dramatically different devolatilization behavior in that at low pressures (<

220   ~1.5 GPa) almost all carbon is released in the form of a methane-rich fluid, an effect that may

221   be of some interest but effectively eliminates decarbonation as a mechanism for explaining

222   island-arc decarbonation. These considerations suggest that predictions based on the neutral

223   bulk redox state initial condition are likely to be characteristic of natural conditions and, to a first

224   approximation, account for the presence of organic carbon in marine sediments (Bebout, 1995).

225

226   Sulfur is an important, but oft neglected, component of subduction zone volatile budgets

227   (Pokrovski and Dubrovinsky, 2011; Evans et al., 2014; Kagoshima et al., 2015; Canil and

228   Fellows, 2017). To evaluate the effect of Sulfur, the GLOSS composition (Table 1) was modified

229   by the addition of 0.1 mol S_2/kg. The sulfur is presumed to be accommodated in pyrite (~0.6 vol

230   %) and the bulk oxygen content reduced accordingly, i.e., the bulk molar O_2 content is reduced

231   by half the molar S_2 content. The possibility of the presence of oxidized sulfur in the initial bulk

232   composition was not considered because in preliminary calculations sulfates were not predicted

233   to coexist with graphite + carbonate at surface conditions.

234

235   The DEW/HKF data base (Shock and Helgeson, 1988; Sverjensky et al., 2014) includes 28 C-

236   O-H-S solute species. In initial calculations the concentrations of glycolate ($C_2H_3O_3^-$), glutarate

237   ($C_5H_7O_4^-$), and lactate ($C_3H_5O_3^-$) were implausibly high at all conditions of interest. Accordingly,

238   these species were not considered in the H_2O-solvent model calculations. In mixed-volatile

239   solvent calculations (the COHS-solvent model), none of the DEW/HKF C-O-H-S solute species

240   were considered, and the solvent was initially treated as a mixture of H_2O, H_2, CO, CO_2, CH_4,

241   SO_2, and H_2S species. These calculations demonstrated that H_2, CO_2, CH_4, SO_2, and H_2S had

242   no significant effect on solute speciation or bulk chemistry. The final calculations considered

243   only the four dominant species (H_2O, CO_2, CH_4, and H_2S).

244

245   Results are presented for closed system sediment devolatilization computed by lagged

246   speciation with the COHS-solvent model. These results are compared to four variants to

247   illustrate technical differences and to inform the devolatilization process. Specifically, the

248   variants, and their purposes, are: 1) simple back-calculation, to contrast the lagged- and back-

249   calculation methods; 2) H_2O-solvent, to illustrate the consequences of the choice of solvent

250   model on fluid speciation and chemistry; 3) fluid-fractionation, a more realistic open-system

251   model for devolatilization; and 4) infiltration-driven devolatilization, an effective, if poorly

252   constrained, mechanism for slab-decarbonation.

253

254   Thermodynamic details of the model calculations and the implementation of the DEW/HKF

255   formulation are summarized in the Appendix. The computer program and data files used for

256   these calculations are available at www.perplex.ethz.ch.

4.1 Devolatilization vs Dissolution

258   The difference between the phase proportions predicted for GLOSS subduction models that

259   account for both devolatilization and dissolution (Fig 4a) as opposed to a model without

260   dissolution (Fig 4b) is surprisingly large. Most notably in the absence of dissolution white mica

261   undergoes no significant dehydration. In contrast, in the lagged speciation model, mica is almost

262   completely dehydrated at the maximum pressure, 6.6 GPa, of the profile. Likewise, without

263   dissolution, the proportions of pyrite and aragonite are approximately constant after dolomite is

264   destabilized at ~5 GPa, but in the lagged speciation model pyrite and aragonite are eliminated

265   by dissolution at 6.4 GPa. The maximum pressure at which phase relations are computed in the

266   lagged-speciation calculation is the point at which the fluid composition becomes so solute-rich

267   that the rock-dominated limit (Fig 2) is violated.

268

269   Although not easily visible (Fig 4b), the volume of diamond increases ten-fold, to ~0.1%, over

270   the same interval that aragonite begins to dissolve. From the fluid speciation (Fig 5a), it is

271   apparent that this phase of diamond precipitation is related to an increase in the concentration

272   of $CaSO_4$ in the fluid, which forms by the reduction of carbon bound in aragonite. This prediction

273   is consistent with the observation of sulfate species and solid carbonate in fluid inclusions in

274   natural subduction zone diamonds (Frezzotti et al., 2011). In calculations not reproduced here,

275   Aragonite and mica are destabilized at essentially the same conditions for the S-free GLOSS

276   composition; therefore, this process is not dependent on the stability of aqueous $CaSO_4$ and the

277   oxidation of pyrite.

278

279   As anticipated by earlier studies (Manning et al., 2013; Galvez et al., 2015), dissolution roughly

280   doubles carbon loss (Fig 6a). In early models of slab-decarbonation (Kerrick and Connolly,

281   2001ab), closed system results were used to estimate carbon transfer under the assumption

282   that the accumulated fluid is released in a single batch at sub-arc depth. On a global scale the

283   fluid-mediated mass transfer of element i is

284
$$Q_i = v_s h_0 \rho_0 N_i n_i$$
12

285   where v_s is the global subduction rate (2.7 km²/y, Stern, 2002), h_0 and ρ_0 are initial thickness

286   and density of the source rock, N_i is the atomic weight, and n_i is the number of moles of element

287   released by a unit mass of the source rock (Fig 6a). For present purposes, it is assumed that

288   the bulk of the slab carbon is contained in a 1300 m thick section consisting of 800 m of GLOSS

289   sediment (Plank and Langmuir, 1998) and 500 m of hydrothermally altered basalt (Staudigel et

290   al., 1989). Both lithologies have comparable initial carbon content (0.7 mol/kg) and density

291   (2600±100 kg/m^3) in which case the carbon input by subduction of oceanic crust is 76 Mt/y,

292   which lies within the range of recent estimates (35-88 Mt/y; Kerrick and Connolly, 2001a;

293   Dasgupta and Hirschmann, 2010; Kelemen and Manning, 2015). To make a first order

294   assessment of the global carbon-loss, it is assumed that carbon-loss in the basalt section is

295   comparable to that computed for GLOSS sediment. Justification for this assumption follows from

296   the mineralogical similarity of sedimentary and basaltic eclogites (Kelemen and Manning, 2015).

297   Based on these assumptions the global carbon loss for batch devolatilization with ($n_C = 0.28$

298   mol/kg, Fig 6a) and without ($n_C = 0.12$ mol/kg) dissolution is 30.6 Mt/y and 13.1 Gt/y, these

299   values compare with estimates of island-arc carbon emissions (18-55 Mt/y, Kerrick and

300   Connolly, 2001a; Dasgupta and Hirschmann, 2010; Kelemen and Manning, 2015). At face

301   value, this result suggests dissolution resolves the mismatch between predicted carbon loss and

302   the observed carbon emission; however, that conclusion is not justified in light of model

303   uncertainty. For example, an increase of 100 K, which is well within the uncertainty of

304   geodynamic model predictions (Gerya et al., 2002), in sub-arc temperatures of the model

305   geotherm (Fig 3) causes a five-fold increase in C solubility for a molecular fluid model (Connolly

306   2005). While electrolytic chemistry moderates this increase (Galvez et al., 2015) it is likely that

307   such thermal effects dwarf the effect of dissolution. Thus the oft stated criticism that simple

308   devolatilization models are incapable of explaining island arc CO_2 emissions is misplaced. The

309   legitimate criticism of closed system models for assessing decarbonation is that the implied

310   batch mechanism for fluid release is physically implausible.

311

312   Although the closed system model does not provide a realistic basis for assessment of slab-

313   mantle mass transfer during subduction. Such models generally provide an upper limit for mass

314   transfer effected without the infiltration of externally derived fluids (Kerrick and Connolly, 2001b).

315   As such, the closed system model suggests that devolatilization processes have the potential to

316   deplete K, H and S from subducted sediments, and almost no capacity to effect Fe or Al mass

317   transfer. The immobility of Al is at odds with experimental observation (e.g., Tsay et al., 2017)

318   and may merely reflect the current limitations of the solute-species model.

319   ## 4.2 Simple Back-Calculated vs Lagged Speciation

320   Simple back-calculated speciation (Galvez et al., 2015) assumes the mineralogy and solvent

321   chemistry obtained by a solute-free phase equilibrium model (e.g., Fig 4b), as such the simple

322   back-calculated model cannot account for the effects of dissolution on mineral stability.

323   However, it is appropriate to compare the lagged and back-calculated fluid speciation to assess

324   the accuracy of back-calculation as an approximation of fluid chemistry. This comparison (Fig

325   5a) is reassuring in that, at conditions within the rock-dominated regime (i.e., pressure < 6.7

326   GPa), the simple back-calculated speciation is generally accurate to within a factor of two or

327   better. Thus, the only prominent disadvantage of simple back-calculation is that it provides no

328   means of recognizing the conditions at which the assumption of a rock-dominated regime is

329   invalid.

330   ## 4.3 H2O- vs COHS-Solvent

331   Comparison of phase equilibria computed for the H_2O- and COHS-solvent models (Fig 4a, Fig

332   5b, Fig 6b) reveals only minor differences. Both models predict CO_2 as the only major C-O-H-S

333   species (Fig 5b). Of the 25 C-O-H-S solute species considered in the H_2O-solvent model only

334   formate ($HCOO^{2-}$) is predicted to be stable at concentrations in excess of 10^{-2} m, a prediction

335   consistent with the observation that formate is observed as a prominent abiotic species in sea-

336   floor hydrothermal systems (Lang et al., 2018). Although no C-O-H-S solute species were

337   included in the COHS-solvent calculation, the use of a mixed-volatile solvent model, does not

338   preclude the simultaneous treatment of additional molecular volatiles as solutes.

339

340   From a computational perspective the advantage of the H_2O-solvent model is that it is

341   inexpensive and accurate in the limit of dilute molecular solute concentrations. The chief

342 disadvantage of the model is that it cannot be used predict phase separation, for example, the

343 coexistence of H_2O- and CH_4- or CO_2-rich fluids (Fruh-Green et al., 2004). The availability of

344 molecular equations for mixed-volatile solvents makes the prediction of phase separation

345 possible; however, in practice, extrapolation of the HKF/DEW formulation to treat non-aqueous

346 solvents is largely untested.

4.4 Open vs Closed System Devolatilization

348 The open system model corresponds to Rayleigh fractionation of the fluid phase. This simulates

349 a scenario in which fluid generated by sediment devolatilization is lost immediately to the mantle

350 wedge and that the sediments are isolated from any fluids produced at greater depth by

351 channelized flow. The mass-loss for this model (Fig 6c) is roughly an order of magnitude below

352 the solute mass present in the fluid for the closed system model (Fig 6a), yet the fluid speciation

353 of both models is nearly identical (Fig 5c). Thus the difference between the models is that the

354 open system mass-loss reflects solubilities at the time of fluid generation. That mica is refractory

355 in the open system model demonstrates that its dehydration in the closed system model is due

356 entirely to dissolution. As fluid generation is caused primarily by the dehydration of stilbite and

357 lawsonite at low pressure, the open system fluid chemistry is dominated by Na and, to a lesser

358 extent, Si and carbonate species.

359

360 The lagged fluid speciation in the closed- and open-system models is virtually identical (Fig 5c)

361 to the pressure at which the rock-dominated limit becomes relevant for the closed system model

362 (~6.7 GPa). The open system model does not reach this limit because the removal of Sulfur

363 from the system stabilizes the calculation. Comparison of the open-system fluid speciation with

364 that obtained for back-calculation (Fig 5a) illustrates that use of back-calculated results beyond

365 the rock-dominated limit leads to substantial errors.

366

367   By excluding the possibility of fluid infiltration, the open system represents the most

368   conservative model for subduction zone mass transfer. Based on the assumptions discussed

369   previously in reference to the closed system model, Equation 12 yields global carbon losses by

370   fluid fractionation ($n_C = 0.05$ mol/kg, Fig 6c) of 5.5 Mt/y, of which 1.1 Mt/y is lost at fore-arc

371   depths, at the onset of fluid generation. While the uncertainties are formidable, this result

372   suggests that indeed a simple devolatilization and dissolution process cannot explain island-arc

373   C emissions in the range 18-55 Mt/y (Kerrick and Connolly, 2001a; Dasgupta and Hirschmann,

374   2010; Kelemen and Manning, 2015) and that a fluid-mediated explanation for these emissions

375   requires that the crust be infiltrated by fluids derived by mantle dehydration.

376   ## 4.5 Infiltration-Driven Devolatilization

377   For the subduction zone thermal model adopted here (Rupke et al., 2004), serpentine

378   dehydration occurs top of the slab is at pressures between 3.9 and 4.6 GPa (Connolly 2005).

379   Taking 4.3 GPa as the representative pressure and the metasediment composition obtained

380   from the open system model at that condition (Table 1), the infiltration-driven mass transport is

381   assessed under the assumption that the fluid released by serpentine dehydration is, and

382   remains, pure water until it reaches the sediments. This assumption is unlikely to be true for

383   elements such as Na and Si, which are abundant in the igneous crust, but it is a reasonable first

384   approximation for K and C which are concentrated in the thin (~1300 m) package of altered

385   basalt and sediment atop the subducted slab (Staudigel et al, 1989; Alt & Teagle 1999). The

386   thinness of this package is taken as justification for reducing the problem to a zero-dimensional

387   model. Models in which the fluid is generated within, and infiltrates through, a subducted

388   metamorphic column are tractable (Connolly 2005; Gorman et al., 2006), but too complex for

389   presentation here.

390

391   The initial fluid speciation in the zero-dimensional infiltration model (Fig 7b) is slightly different

392   from the speciation for the open system model (Fig 5c) at the same pressure because the

393   addition of pure water eliminates the small amount of diamond that is ubiquitous in the previous

394   models and stabilizes oxidized sulfur species ($CaSO_4$, HSO_4^-, HSO_3^-). The infiltration model

395   indicates that ~23 mol of water is required to completely decarbonate a kilogram of GLOSS

396   metasediment (Fig 7c). As serpentinized mantle contains ~13 wt % H_2O or 7.2 mol H_2O/kg

397   mantle, this implies a mass of serpentinite ~3.2 times that of the carbon-bearing oceanic crust is

398   adequate to completely decarbonate the crust. The aforementioned mass is well within

399   estimates for upper limit on the extent of mantle serpentinization (Connolly, 2005).

400

401   The elimination of mica and alkali earth elements by the addition of slightly more water than

402   required for decarbonation leaves lawsonite as the only carrier of water at depths beyond the

403   conditions of serpentine dehydration. With continued subduction lawsonite would dehydrate (Fig

404   4), leaving the metasediment completely depleted in alkali earth elements, and hydrogen and,

405   thereby, refractory to melting. By neglecting the effect of the igneous crust on the chemistry of

406   mantle derived fluid, the present model likely exaggerates Na-depletion. This model defect is

407   less likely to be important for potassium, which correlates strongly with hydrogen, because of its

408   greater solubility and lower absolute abundance in the igneous crust. Thus, the result suggests

409   an anti-correlation between the efficacy of infiltration-driven decarbonation and slab melting.

410   Unfortunately, there are many reasons why slab melting (Behn et al., 2011) is sporadic, and

411   therefore its absence is not an argument for the importance of infiltration-driven decarbonation.

412

413   The complete depletion of C, K, and Na in the infiltration-driven model may seem to contradict

414   the rock-dominated limit of the lagged speciation algorithm. This is not the case, as in the simple

415   open-system model, because the elements depleted from the condensed phases of the system

416   are removed with the fluid.

5. Discussion

The lagged-speciation algorithm derives extraordinary efficiency by using back-calculated fluid speciation (Galvez et al., 2015) to predict the stable composition of electrolytic fluids during Gibbs energy minimization. The cost of this efficiency is that the algorithm fails if the predicted fluid composition is inconsistent with mass balance constraints. While there is no remedy for this condition, the conditions can be recognized, making it apparent when reformulation of the solvent model or a more rigorous algorithm (e.g.: Harvie et al., 1987; Karpov et al., 2001) is required. The limitation of the algorithm related to this failing is that it cannot treat situations in which an element is present only in the form of a solute species. In the case C, O, H, and S, which appear both as molecular fluid species and common mineral constituents, this limitation can be circumvented by reformulating the solvent model to include these elements. Halogens are more problematic. There are equations of state that describe brines in terms of a solvent standard state for NaCl (Driesner and Heinrich, 2007; Aranovich et al., 2010; Dubacq et al., 2013), the complication in integrating such equations of state with solute speciation models such as the HKF is to define a relation between the macroscopic and microscopic NaCl content and to account for the resulting non-linearity in activity-composition relations. This complication has not been addressed in the current computer implementation of the lagged speciation algorithm.

In geochemical implementations of the HKF/DEW formulation water is the sole solvent and molecular volatiles and organic species are described by a solute standard state. In contrast, Galvez (2015) adopted a solvent standard state for the dominant carbonic volatile species. Both solvent formulations offer advantages in specific situations, but in the general case of a miscible water-rich solvent phase both formulations are shown here to produce comparable results (Fig 5b).

442

Because the primary concern of this paper is methodological, no attempt has been made to

assess the accuracy of the published thermodynamic data used for the calculations presented

here. This data is subject to significant random sources of error, but a bias toward under-

prediction of mineral solubility is inherent in microscopic speciation models due to the existence

of unanticipated species (Manning, 2007; Pokrovski and Dubrovinsky, 2011; Manning et al.,

2010; Tumiati et al., 2017). Sverjensky et al. (2014) demonstrated that the current data is

capable of reproducing experimental solubility data in two-component systems at subduction

zone pressure conditions; however, in systems with chemistry approaching that of natural rocks,

thermodynamic models underestimate the concentrations of Ca, Al, Fe, and Mg by orders of

magnitude (Galvez et al. 2015). Although this error is significant, the absolute concentrations of

these elements, with the probable exception of Al, is small compared to those of the alkali-earth

elements at subduction zone conditions (Tsay et al., 2017).

With the aforementioned caveats, accounting for electrolytic fluids does not profoundly change

assessments of the efficacy of fluid-mediated decarbonation during subduction based on

classical molecular fluid models because carbonic molecular species remain prominent, if not

dominant, in electrolytic fluids. The behavior of sulfur is more surprising. At fore-arc conditions S

is nearly insoluble and accommodated primarily as H_2S at fore-arc conditions. The present

modeling (Fig 5) suggests that sulfur solubility rises at sub-arc conditions due to the stability of

oxidized sulfur species that form by the reduction of carbonate to diamond (Frezzotti et al.,

2011). This rise in solubility is intriguing as a mechanism for transferring an oxygen excess to

the mantle wedge.

The present models reconfirm the conclusion that sub-solidus devolatilization, as an isolated

process, cannot explain extensive slab decarbonation. Gorman et al. (2006) is often cited to

468 support the contention that carbonate also remains in more elaborate infiltration-driven models

469 of slab-decarbonation. However, the behavior in those models was influenced by the choice of

470 an anomalously young slab age. Because the top of subducted slabs is heated rapidly after the

471 slab mantle becomes detached from the lithosphere (Rupke et al., 2004), carbon-solubility rises

472 to a maximum near sub-arc depths for typical subduction zone conditions (Connolly 2005; Fig 6

473 here). Slab age is important in this context because it controls when serpentine dehydration, the

474 putative source of infiltrating fluid, is released. For subduction models based on a slab age close

475 to the global average, there is no difficulty in explaining island-arc CO_2 emissions in terms of an

476 infiltration-driven scenario for decarbonation (Connolly 2005; Fig 7 here). The concern over

477 whether such models are capable of quantitatively explaining decarbonation is misplaced.

478 Rather, the weakness of the infiltration-driven scenario is the assumption that large volumes of

479 mantle-derived fluid equilibrates pervasively with the subducted crust. The value of

480 incorporating electrolytic fluid chemistry in a model of the infiltration-driven devolatilization is that

481 it offers a complete geochemical picture of the infiltration process and thereby may provide

482 arguments for the rejection or acceptance of the mechanism. In particular, the present modeling

483 suggests that is likely that any infiltration event capable of depleting carbon from the subducted

484 crust would effectively desiccate the crust by potassium depletion and render the crust

485 refractory with respect to melting.

Acknowledgements

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614

Figure Captions

615 Figure Captions

616 Fig 1. Schematic specific Gibbs energy (g) vs composition (x_{SiO2}) diagram for the H_2O-SiO_2

617 system illustrating conditions for failure of the lagged speciation algorithm as discussed in the

618 text.

619

620 Fig 2. True (a) and algorithmic representation (b) of phase relations in the $CaSiO_3$-SiO_2-H_2O

621 system with a one-component solvent (H_2O), wollastonite, quartz, and fluid as possible phases

622 illustrating conditions for failure of the lagged speciation algorithm as discussed in the text.

623

624 Fig 3. Geotherm assumed for the subduction zone models (Ruepke et al. 2004).

625

626 Fig 4. Volumetric phase proportions during closed-system devolatilization of the GLOSS

627 sediment composition (Table 1) computed by (a) lagged speciation and (b) without taking into

628 account dissolution. The lagged speciation results compare the COHS-solvent model (solid

629 curves) and the H_2O-solvent model (dashed curves) commonly assumed in applications of the

630 DEW/HKF formalism. The fields for small amounts of graphite, potassium feldspar,

631 clinoamphibole, and pumpellyite, which are stable at low pressure, are not labelled. Mineral

632 proportions (not shown) computed for the open-system devolatilization model are essentially

633 identical to those obtained by neglecting dissolution. Phase notation and solution models are

634 summarized in Table 2.

635

636 Fig 5. Fluid speciation in various models for the devolatilization of the GLOSS sediment

637 composition. (a) Closed-system devolatilization with the COHS-solvent model, comparing the

638 lagged (solid curves) and simple back-calculated (dashed curves) speciation. (b) Closed-system

639 devolatilization using lagged speciation, comparing the COHS- (solid curves) and H_2O-solvent

640   (dashed curves) models. (c) COHS-solvent using lagged speciation, comparing open- (diamond

641   symbols) and closed-system (solid curves) devolatilization. In simple back-calculation, fluid

642   speciation is calculated post-hoc from the solute-free phase equilibrium model (Fig 4b), thus the

643   phase proportions and fluid composition violate mass balance. Nonetheless, the back-

644   calculated speciation is accurate to within a factor of two within the rock-dominated limit (i.e., at

645   pressure < ~6.7 GPa).

646

647   Fig 6. Mass present in, or removed by, the fluid generated during devolatilization of 1 kg of

648   GLOSS sediment in various models. (a) Closed system: COHS-solvent, lagged speciation (solid

649   curves) vs COHS molecular fluid (dashed curve for C). (b) Closed system, lagged speciation:

650   COHS-solvent (solid curves) vs H_2O-solvent (dashed curves). (c) Open system: COHS-solvent

651   (diamond symbols) vs COHS molecular fluid (circular symbols for C); symbols indicate the

652   points along the subduction path at which fluid was generated. In closed system models, the

653   mass of a component present in the fluid may decrease with pressure due to changing

654   solubility; in the open system model, mass loss is irreversible.

655

656   Fig 7. Phase proportions (a), fluid speciation (b), and mass loss (c) for the infiltration-driven

657   devolatilization model. Phase notation and solution models are summarized in Table 2.

658

Tables

Table 1. Average subducted sediment composition (GLOSS, Plank and Langmuir, 1989). The GLOSS composition has been modified by the addition of sulfur corresponding to the presence of ~0.1 volume % pyrite, the original O_2 content has been recomputed so that the bulk composition is redox neutral. The metasediment composition is the bulk composition obtained at 4.3 GPa from the GLOSS composition by open-system devolatilization (Fig 6c).

	Initial GLOSS Sediment		Metasediment at 4.3 GPa	
	mass fraction, %	mol/kg	mass fraction, %	mol/kg
H_2	0.823	4.085	0.197	0.978
C	0.824	0.686	0.847	0.706
Si	27.621	9.835	29.317	10.439
Al	6.369	2.360	6.802	2.521
Fe	4.112	0.736	4.392	0.786
Mg	1.520	0.625	1.623	0.668
Ca	4.285	1.069	4.551	1.135
Na	1.809	0.787	1.804	0.785
K	1.735	0.444	1.798	0.460
O_2	50.578	15.806	48.322	15.101
S_2	0.323	0.101	0.345	0.108

667 Table 2. Mineral notation, formulae and solution model sources (1 - Green et al., 2016; 2 -

668 Holland and Powell, 1998; 3 - Fuhrman and Lindsley, 1988; 4 - Jennings and Holland, 2015; 5 -

669 Chatterjee and Froese, 1975). See Appendix for condensed phase and fluid species

670 thermodynamic data sources.

671

Symbol	Solution	Formula	Source
Amph	clinoamphibole	$Ca_{2(y+u+v)}Na_{u+2(w+z)}[Mg_xFe_{1-x}]_{7-3u-2v-4(w+z)}Fe_{2z}Al_{4y+3v+2w}Si_{8-(y+v)}O_{22}(OH)_2$	1
arag	aragonite	$CaCO_3$	
cc	calcite	$CaCO_3$	
coe	coesite	SiO_2	
Cpx	clinopyroxene	$Na_{y+w}[CaMg_xFe_{1-x}]_{1-y-w}Al_yFe_wSi_2O_6$	1
Dol	dolomite	$CaMg_xFe_{1-x}(CO_3)_2$	2
F	fluid		
Fsp	feldspar	$K_yNa_xCa_{1-x-y}Al_{2-x-y}Si_{2+x+y}O_8$	3
Grt	Garnet	$[Fe_xCa_yMg_{1-x-y}]_3[Fe_{1-v}Al_v]_2Si_3O_{12}$	4
ky	kyanite	Al_2SiO_5	
law	lawsonite	$CaAl_2Si_2O_6(OH)_2$	
M	magnesite	$Mg_xFe_{1-x}CO_3$	2
Ms	muscovite	$K_xNa_{1-x}[Mg_{1-v}Fe_v]_yAl_{3-y}Si_{3+y}O_{10}(OH)_2$	5
Pu	pumpellyite	$Ca_4Mg_xFe_{1-x}[Fe_yAl_{1-y}]_5Si_6O_{21}(OH)_7$	ideal
q	quartz	SiO_2	
stlb	stilbite	$CaAl_2Si_7O_{11}(OH)_{14}$	
Stlp	stilpnomelane	$K_{0.5}[Mg_{1-x}Fe_x]_5Al_2Si_8O_{18}(OH)_{12.5}$	ideal
stv	stishovite	SiO_2	

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Computed phase changes, fluid speciation, and mass loss as a function of water infiltration through metasediment at sub-arc conditions.
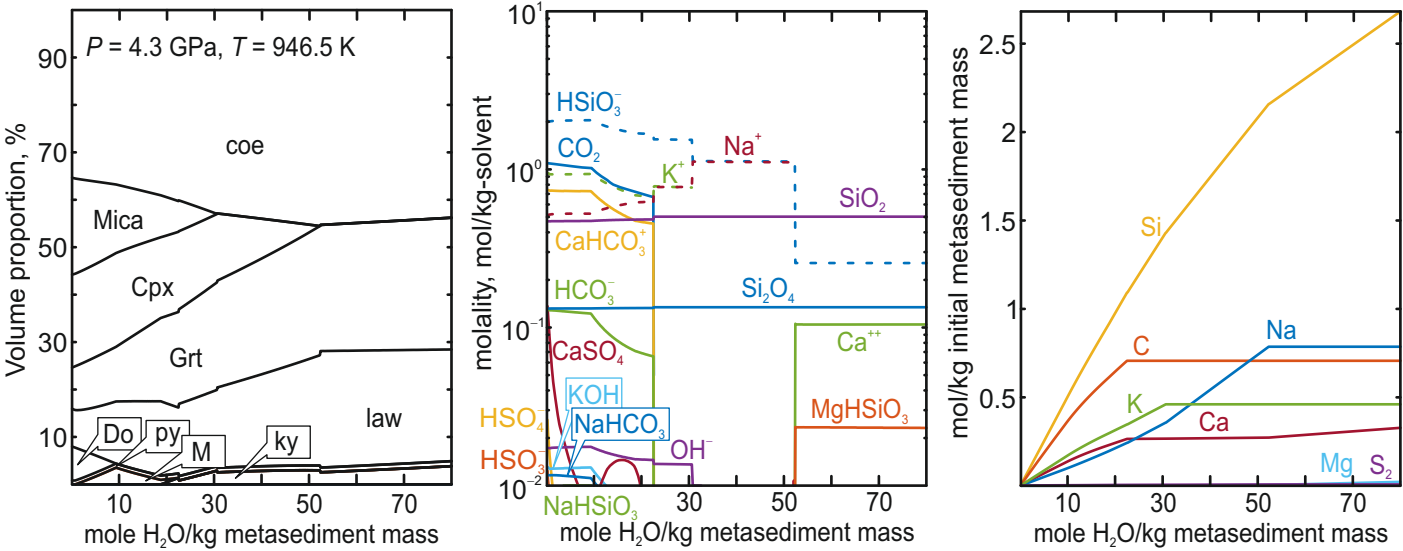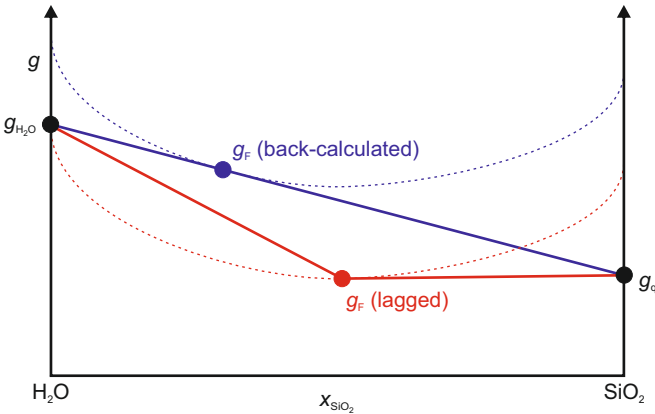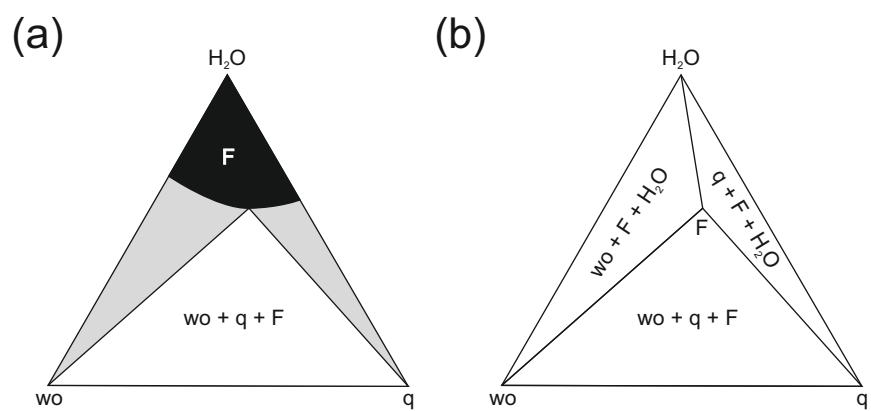
Figure 1

g

g_{H_2O}
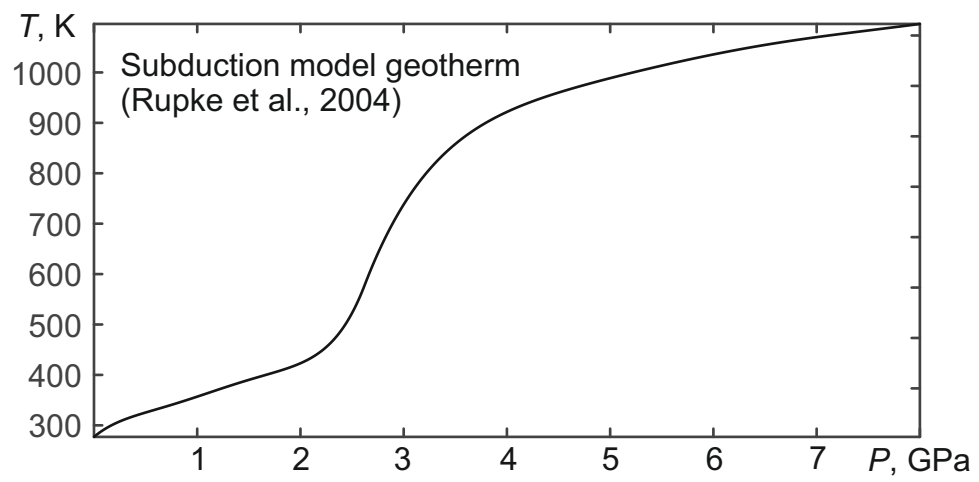
g_F (back-calculated)

g_F (lagged)

g_q

H_2O

x_{SiO_2}

SiO_2

Figure 2

(a)

H$_2$O

F

wo + q + F

wo   q

(b)

H$_2$O

wo + F + H$_2$O

q + F + H$_2$O

F

wo + q + F

wo   q

Figure 3

Figure 4

Figure 5

(a) Closed system, COHS-solvent
- back-calculated
- lagged

(b) Closed system, lagged
- COHS-solvent
- H2O-solvent

(c) Lagged, COHS-solvent
- ◇ ◇ ◇ open
- closed

Figure 6

(a)

(b)

(c)

Figure 7

(a) H₂O infiltration at $P = 4.3$ GPa, $T = 946.5$ K

Volume proportion, %

coe

Mica

Cpx

Grt

law

Do py M ky

mole H₂O/kg initial metasediment mass

(b)

molality, mol/kg-solvent

HSiO₃⁻
CO₂
K⁺
Na⁺
SiO₂
CaHCO₃⁺
Si₂O₄
HCO₃⁻
Ca⁺⁺
CaSO₄
MgHSiO₃
KOH
HSO₄⁻
NaHCO₃
HSO₃⁻
OH⁻
NaHSiO₃

mole H₂O/kg initial metasediment mass

(c)

mol/kg initial metasediment mass

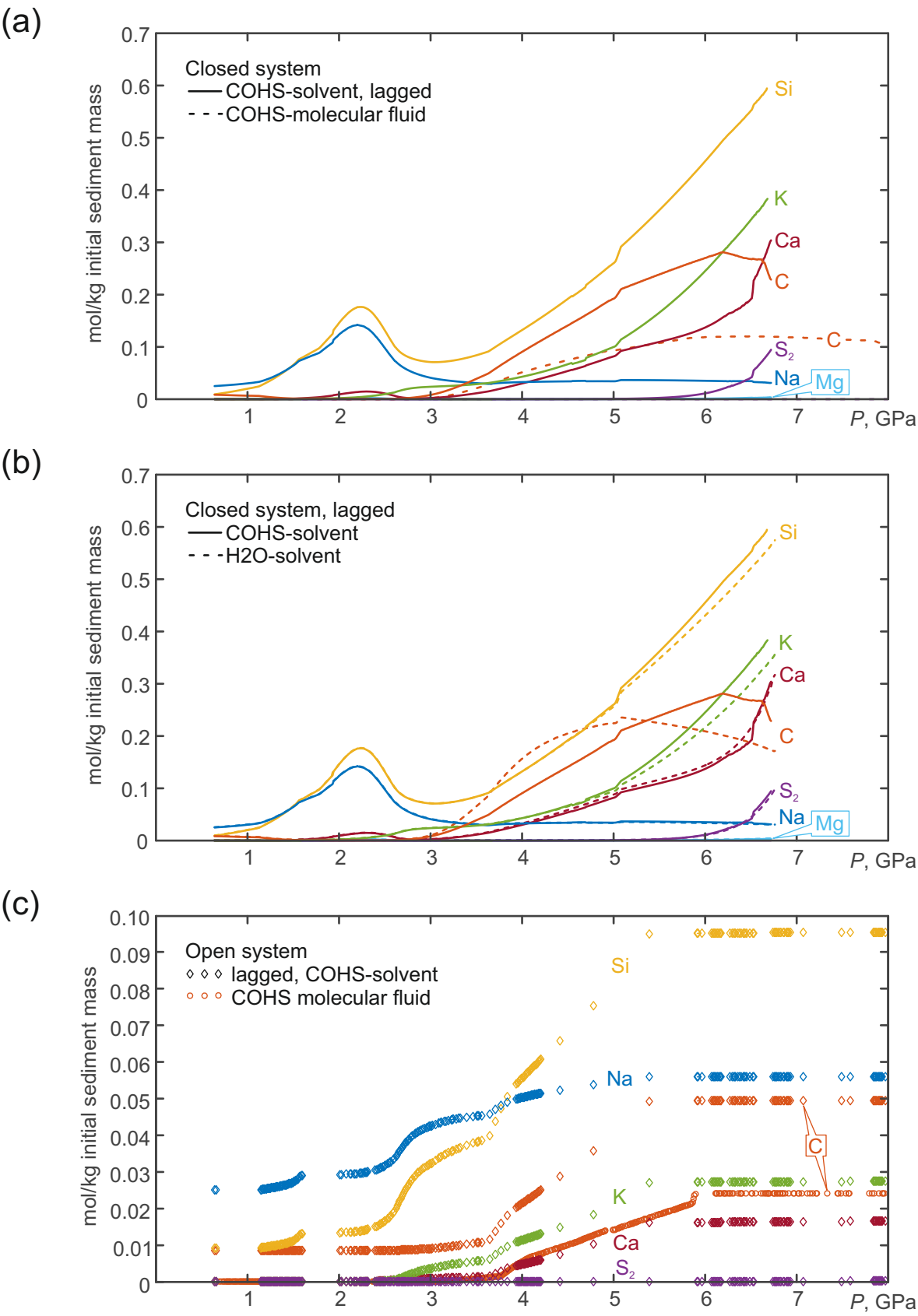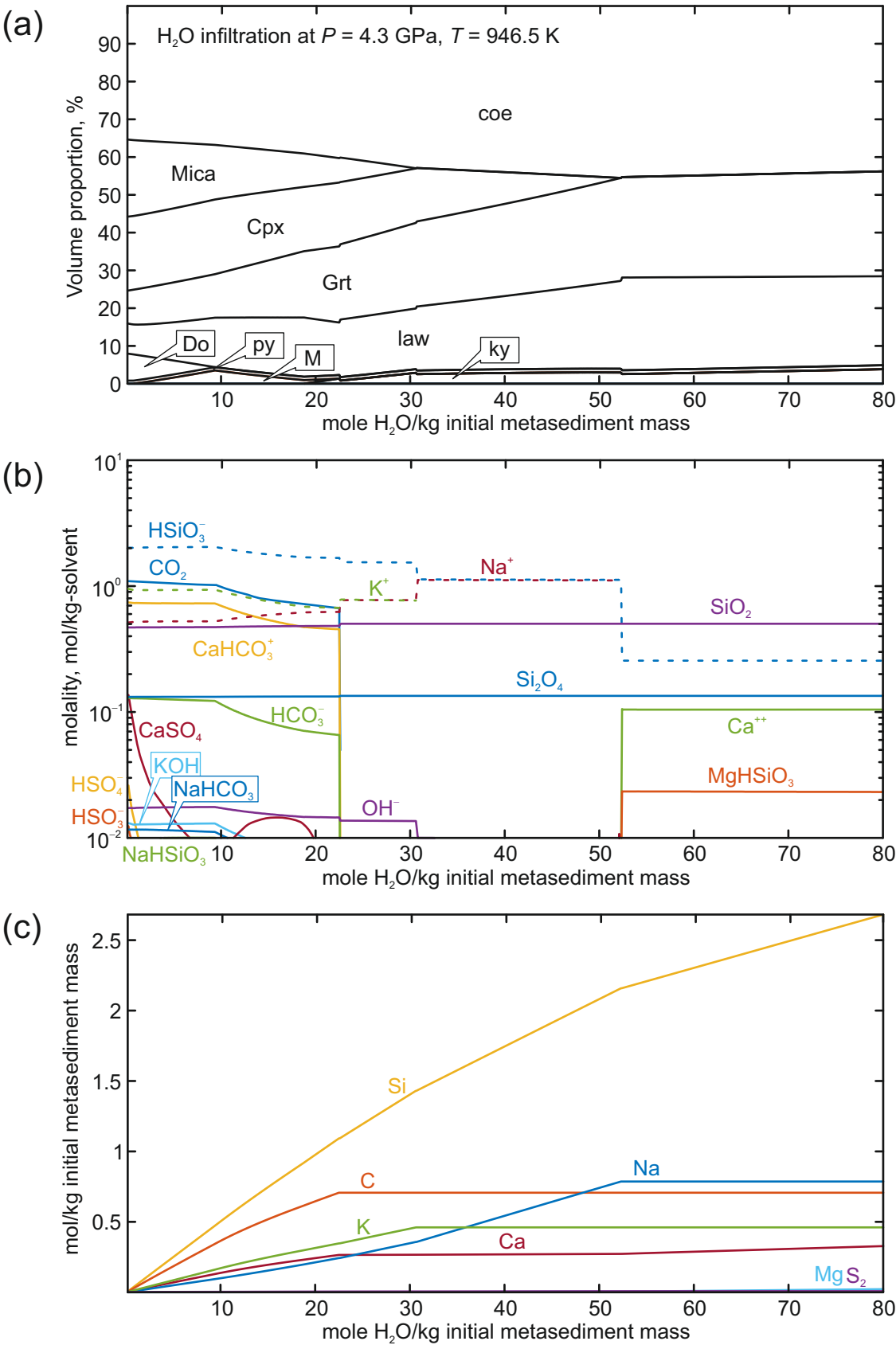Si

C

K

Na

Ca

Mg S₂

mole H₂O/kg initial metasediment mass

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